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Math Teachers Press, Inc.

Curriculum at a Glance

Grades K-8 in English and Spanish



Description

Moving with Math® Extensions is a condensed grade-level program designed to teach the underlying concepts of essential standards. An easy-to-use, integrated system links all learning objectives to tests, teaching activities, and reteaching pages.

Pacing calendars and clear, lightly-scripted lesson plans ensure that teachers know exactly what to do and say each day. Every lesson uses manipulatives to guide students as they explore each math concept.

Classroom Kits

Classroom kits are available in English and Spanish for Grades K to 8. Each kit comes in a colorful carrying box with a Teacher Resource Manual, 20 student activity books, 20 Pre-and-Post Tests and record sheets, and 20 Parent Handbooks. Manipulative kits are purchased separately.

State and National Standards

The *Moving with Math*[®] curriculum embraces NCTM curriculum guidelines, and has been correlated to most state and national standards. Call for your state correlation.

Flexible Time Frame

The program may be used in summer schools from 4 to 6 weeks and extended day classes from 20 to 80 hours by varying the activities to fit the time available for each lesson. The Teacher Manual includes a 20-lesson pacing plan, and 30-lesson plans are also available.

Parent Handbooks

Based on the recommendations of the No Child Left Behind Act, Parent Handbooks provide everything a teacher needs to connect to home. Handbooks share Pre-Test results with parents, give an overview of the program, and contain fun games and activities for parents and students to do together at home.

Professional Development

Educators may choose from a variety of options to fit their needs and budget. Professional Development Kits, training DVDs, and workshops with our educational consultants or your in-house trainers are available. All training is content-focused and is designed to help teachers reach students who have low test scores.

Boxed Classroom Kits

Each boxed classroom kit contains all the printed materials teachers need for a fun and successful extended day or summer school. Manipulative kits are purchased separately.

Each boxed kit contains:



1 Teacher Manual

- A Pacing Calendar to help teachers stay on track.
- **Objectives** matched to test items and teaching pages.
- Reproducible Pre- and Post-Tests.
- Writing Prompts with a reproducible journal for each student.
- Activity-Based Lessons for an interactive learning environment.
- Games to make learning fun and keep students engaged.
- **Reproducible Reteaching Pages** for all grade-level objectives.



20 Student Activity Books

- Activity Pages that match the lessons in the Teacher Manual.
- 32 Daily Reviews to reinforce all grade-level objectives.
- Review Record Sheet for continuous tracking of individual progress.



1 Test Assessment Pack

- 20 Pre- and Post-Tests matched to grade-level objectives.
- 20 Student Progress Reports to gauge progress or use as a report card.
- Class Record Sheet for easy tracking of class progress.
- Final Test Journal Prompt.



20 Parent Handbooks

- **20 Parent Handbooks** with a parent letter, a record of the student's strengths and weaknesses, plus games and activities to do at home.
- 20 Certificates of Achievement



Hands-on Math

Every fun and engaging lesson guides students through the three stages of learning:



Students use manipulatives to understand math concepts.

Multi-Digit Numeration

To develop understanding of multi-digit numeration, students practice these activities:

- Writing numerals from blocks. Display a set of ones, tens, and hundreds blocks. Ask students to describe and record what they see.
- 2. Building blocks from numerals. Write a 3-digit numeral. Ask students to read the number. Then ask them to build the number with base ten blocks.
- **3. Building blocks and writing numerals from oral presentation.** Say a 3-digit number out loud. Students build the number and write the numeral.

Introducing Fractions

These activities help students gain an understanding of fractions. Students translate between concrete models, pictures, and spoken words.

- Display a fraction bar. Ask 3 questions: How many parts has the whole been divided into? How many parts are shaded? What fractional part is shaded?
- Write a fraction on the board, e.g., ³/₄. Have students draw a picture of this fraction.
- **3.** Say a fraction name, e.g., ⁷/₁₂. Have students find a bar to match the fraction and then draw a picture of that fraction.



4. Drawing pictures of numerals. Students draw pictures using a small square for each hundred (■), a stick for each ten (I), and a dot for each one (.).



What's My Secret? Partners take turns selecting a set of fraction bars alike in one way. The partner guesses the secret similarity.

The Moving with Math® Way

Problem Solving Every Day

FOR Problem Solving: The Hands-on Difference

Students discover the conceptual underpinnings of math using manipulatives. Research proves that students who use manipulatives have higher scores on achievement tests and are better problem solvers.





ABOUT Problem Solving: Explicit Steps and Strategies

Students develop and apply a five-step problem solving model. They discover that a variety of strategies may be used to solve the same problem.

Image: Constraint of the second of the se	<section-header> Brobem Solving: Use Different Strategies List the rurbers of the strategies you can use to solve each protein List the rurbers of the strategies you can use to solve each protein I. if a car travels 30 miles per hour, how far will it go in 16 hours? Strategies Attail Strategies Strategies Strategies Strategies</section-header>	
4 Estimate Vivue about 20 more shells on Saturday than on Sunday.	Strategies Strategies Estimate Actual Estimate Actual Strategies In The distance to the Scout camp is 130 miles Her area noids 4 Scouts and ther camping geat, how many cars will be needed? In The distance to the scout camp is 130 miles Her area	
s Sons and encotions 21 problem again: Gally found 21 more shells on Saturday than on Sunday.	Strategies Strategies Actual Estimate Actual 14	Alt minimi e tana a mun

VIA Problem Solving: Real-World Problems

Lessons begin with problems from the teacher guide, the student page, or those written by the teacher or student. As students write word problems, they understand the structure of a word problem and the need to focus on the question—the main point in the problem.

The Moving with Math[®] Learning System

Assessment Linking...

Standards to Tests, Curriculum, and Home.



Using our teacher-friendly curriculum:

The *Moving with Math*[®] Extensions is a condensed, grade-level curriculum for grades K–8. The series follows a systematic organization that is modeled in the diagram above. The series begins with a set of objectives that are correlated to state and national standards. These objectives are assessed with a Pre-Test before the course begins and results are interpreted with helpful record sheets. Teachers can then connect with home and share findings and learning objectives with parents.

Next, teachers use manipulative-based lesson plans to teach key math concepts, skills, and problem solving. Throughout the course of instruction, teachers monitor progress and assign reteaching with Daily Reviews and *Skill Builders*.

Finally, a Post-Test measures progress and identifies further intervention needs.

As this sampler guides you through each step, you will be able to see how the curriculum integrates assessment with a coherent structure of skills that fit together to make a complete, hands-on system for teaching math.

Step 1: Learning Objectives

Matching the Standards

Everything starts with learning objectives.

						in the Grade 4 Extensions bool
		Numeration	Student Book	Skill Builders		
	B-1	Identify the place value in a 3-digit number.	1, 2	1-1		
	B-2	Compare and order numbers up to 6 digits.	5, 6	2–1		
	B-3	Complete patterns of multiples of the numbers 1–6 or 10.	8	3–1		
	B-4	Write a 4-, 5- or 6-digit numeral from printed words or sets.	7	4–1		
	B-5	Write the words for any numeral up to 6 digits in length.		5–1		
	B-6	Identify the place value in a 4-, 5-, or 6-digit number.	3, 4	6-1		
	B-7	Round a 2-, 3- or 4-digit number to the nearest ten.	9	7-1		Teachers can see
	B-8	Round a 3- or 4-digit number to the nearest hundred.	10	8-1		where to find early and the second se
	B-9	Find a missing number.	11, 12	9–1, 9–2		objective in the
		Addition				Teacher Guide,
2	B-10	Add 3-digit numbers with zero or two regroupings. Word problems.	13, 23	10-1 49-2, 49-3	′	Student Book, a
gur	B-11	Add three or four 2-digit numbers with regroupings.	14	11-1		reproducible Ski
é N	B-12	Add 4- or 5-digit numbers with regroupings.	15	12–1		Builders pages.
ectiv	B-13	Add up to five numbers of differing lengths, 1- to 5-digits.	16	13–1		
ģ	B-14	Knows the meaning of "sum" and the "+" sign in addition.		14–1		
Iten		Subtraction				
Test	B-15	Subtract 3-digit numbers with up to two regroupings, word problems,	17, 18, 23	15-1.15-2.49-2.49-3		
	B-16	Subtract 3-digit numbers with regroupings across zero.	19	16–1		
	B-17	Subtract 4- or 5-digit numbers with regroupings, can be across zero.	20	17–1		
	B-18	Subtract numbers of varying lengths, 1- to 5-digits.	21	18–1		
	B-19	Knows the meaning of "difference" and the "-" sign in subtraction.		19–1		
		Multiplication				
	B-20	Knows multiplication facts with factors 0-9	05 06 07	20 1 20 2 20 2		
	B-21	Multiply a 3-digit number by a 1-digit number can be across zero	20, 20, 21	21-1 21-2		
	B-22	Multiply a 1- or 2-digit number by 10 or a multiple of 10.	28, 34, 35	22–1		
	B-23	Multiply a 2-digit number by a 2-digit number with rearouping.	20, 07, 00	23–1		
	B-24	Knows the meaning of "product" and the "x" sign in multiplication.		24–1		
	B-23 B-24	Multiply a 2-digit number by a 2-digit number with regrouping. Knows the meaning of "product" and the "x" sign in multiplication.		23–1 24–1		

Learning Objectives and Accountability

Moving with Math[®] learning objectives provide accountability to districts, parents, and students. Learning objectives match both what students need to know for future success and for state and national standardized tests. Call your local representative or (800) 852-2435 for state correlations.

Step 2: Assess

Tests Aligned to Objectives

Pre-Test Identifies Weak Skills, Post-Test Demonstrates Progress



Testing Ensures Accountability

Each question number on the Pre-Test and the Post-Test assesses the same objective at the same difficulty level. For example, Problem 1 on both tests asks students about 3-digit place value. Each test is approximately 50 questions.

Step 3: Interpret

Using Test Results

Help teachers target and individualize instruction.



• The average percent correct for each objective.

Questions are grouped by content strand, so teachers can easily see areas of difficulty.

The Teacher Manual Includes Two Ways to View Results

lon TS

Carol W.

Post-Pam W. Pre-

3. 25%

TOTAL%: Pre- 90 90 COrrectly

answered

X X X

The *Class Record Sheet* is grouped by objective and content strand, so a teacher can instantly recognize class weaknesses. Class Record Sheets also provide data for accountability. The *Student Progress Report* is made for assessing individual progress and identifying at-risk students. It is an excellent tool for creating individualized education plans. **Page 9**

2.70%

mean

Step 4: Connect to Home

Parent Handbooks

Share results and provide activities for home.



Games and Activities

Each activity page matches a major content area taught in class. Simple instructions show parents how math skills are taught.

Parent Direction and Involvement

The parent letter shown here explains how the program works and what parents can do at home to help.

Page 10

Step 5: Teaching Tools

Easy Lesson Planning

Teacher-friendly calendars show everything. Vocabulary develops the language of math.



Step 5: Teaching Tools

Hands-On Lessons

Each lesson is organized in 3 easy parts.

- 1. Introductory Activities direct guided, hands-on exploration.
- 2. About This Page connects the student book activities to the lesson.
- 3. Follow Up Activities provide games and reteaching opportunities.



Each student page matches the same lesson plan page.

Step 6: Review and Reteach

Continuous Reassessment

Spiral Reviews for Long-Term Retention



Optional On-Line Assessment Technology Made Easy!

Standards-Aligned

Moving with Math[®] is aligned to state and national standards.

Easy to Use

User friendly—no software to install. All you need are computers and the internet.

Accountability

District, school, classroom, and individual reports can be generated automatically.



On-Line Tests Students using *Moving with Math* may take their Pre-Test and Post-Test at any internet-connected computer.



Instant Reports Teachers can print timesaving reports that show their class' and students' strengths and weaknesses.



Targeted Instruction Reports give clear direction on using *Moving with Math*[®] to differentiate instruction and increase achievement.

Technology addressing the needs of Response to Intervention provides a blended curriculum experience.

Predictive screening Pre-Test Reports

- Identify students in each tier
- Form learning groups
- Provide Individual Educational Plans (IEPs)

Post-Test Reports

- Measure progress
- Provide accountability
- Indicate future instructional needs



Professional Development

Helping Teachers Reach Under-Prepared Students

Moving with Math[®] Workshops

Teachers learn the proven Moving with Math® method to reach under-prepared students. Strategies include using models, vocabulary development, and problem solving.

Teachers learn how to differentiate instruction using Moving with Math[®] assessments to target instruction on weak areas.

Teachers learn by doing. In our hands-on training, teachers practice key manipulative-based lessons that they will use in the classroom.

Even More Training Options Professional Development Kits

Boxed kits contain all the training materials your staff needs to conduct workshops on their own. Each kit includes a teacher resource manual and



student book, presenter's quide, teacher handbooks, overhead transparencies, overhead manipulative, and a training video with sample manipulative-based lessons.



Training **DVDs**

In many cases, training DVDs are all teachers need to use the curriculum successfully.



Each 30-minute grade-level DVD from K through 8 gives a curriculum overview and demonstrates key manipulative activities with students. Included with each Teacher Manual.

Getting the most out of *Moving with Math*[®] Satisfied customers attribute success to Professional Development.



- "The workshops helped teachers reach students who are struggling in math."
- "Teacher evaluations were positive and indicated
- a great appreciation for the time spent to prepare them for the program."
- "The teachers who taught summer school this year
- have reported student improvement."

Cathleen McStroul Math Program Consultant 4-7 Regional Center for Teaching and Learning Reno, Nevada



Page 16

Friendly Lesson Plans

Objective: To introduce the plus sign. To introduce the equals sign.

Materials: Teddy bear counters, Teddy Bear Storyboard (Master 10), numeral cards (Master 6)

Introductory Activities

Acting Out a Story, Introducing the Plus Sign Have children model and retell the following story using teddy bear counters on the Teddy

Bear Storyboard. There were 4 teddy bears playing in the sand box. One more teddy bear joined them. How many teddy bears are in the sand box?

Ask children to tell you the numbers they heard in this story as you write each number on the chalkboard: 4 1 5.

This is a story about 4 bears, 1 bear and 5 bears. What was the action in the story? (The bears came together in the sandbox.) Very good. We call the operation or process of joining things together "addition". We use a special sign to show that the objects or numbers have been added. We use the plus sign.

Write a big plus sign on the board. Have students make a plus sign by crossing the index finger of each hand. Have a volunteer come to the board and draw the plus sign between the two numbers which were joined together. Repeat with other stories.

Acting Out a Story, Introducing the Equals Sign Have children tell and act out a story on the top part of the storyboard as you record the number sentence on the chalkboard.

Two bears were playing on the slide. One more bear came to play with them. How many were playing on the slide? Record 2, 1 and 3 on the chalkboard.

What sign should go between the 2 and 1? Why? (the plus sign, because we are putting ther 2 numbers) **resent?** (the number in





Page 17

Grade

List of Objectives

Program Objectives

an X in the Pre- and of 1 out a	School
tudent	
	exe eddition word prob-
Numeration Numeration	A-27 Estimate and solve audition word pro- lems. Use strategies.
$ \Box \mathbf{A-1} \text{Match objects} \leq 1 $	problems. Use strategies.
A-3 Compare sets \leq 10 objects of tens and A-4 Write the numeral from sets of tens and	A-29 Solve a subtraction problem asking, "How many more of one than another?"
ones. A-5 Not tested in this level. A-6 Write 5 numbers before or after any	A-30 Skip count by 2's, 5's, 10's to 100.
number ≤ 100. Write a numeral up to 3 digits from printed words. Write words for up to a 3-digit numeral.	Geometry & Measurement A-32 Identify "top" and "bottom." A-33 Identify "inside" and "outside."
 □ A-9 Compare and order numbers to 999. □ A-10 Compare lengths – long or short. □ A-11 Compare objects – large or small. 	$\square \square A-34 \text{Identify "between.}$ $\square \square A-35 \text{Identify "next to."}$ $\square \square A-36 \text{Identify "above" and "below."}$ $\square \square A-37 \text{Identify a square.}$
 A-12 Order 5 lengths. A-13 Identify ordinals first through tenth. A-14 Extend patterns of objects. 	$\square \square A-33 \text{Identify a circle.}$ $\square \square A-39 \text{Identify a triangle.}$
Operations $\square \square A-15$ Add with sums ≤ 10 . $\square \square A-16$ Subtract with differences ≤ 10 .	 □ □ A-40 Identify a rectangle. □ □ A-41 Identify portions of a region as halves. □ □ A-42 Identify portions of a region divided into
A -17 Add up to 3 numbers, sums ≤ 10. A -17 Add with sums ≤ 18. Define "+" and "sum."	$\square \square A-43 $ Select 2 figures with the same shape. $\square \square A-44 $ Select 2 figures with the same size.
A-19 Subtract a 1-digit from a 2-digit numbe \leq 18. Define "" and "difference."	A-45 Not tested in this level. A-46 State the value of coins $\leq 9^{\circ}$. Identify the penny and nickel.
Add 2 numbers, 2 digits and 4 digits regrouping.	A-47 State value of 1-9 dimes and 1-9 pen- nies. Identify the dime.
A-21 Add 2 multiples of 10, car Add two 2-digit numbers, no regroup-	A-48 State value of coins and bills \leq \$2.00. Identify the quarter and half-dollar.
A-23 Not tested in this level.	A-49 Tell time to the half nour. Interpret a date endar.
A-24 Not tested in and A-25 Subtract two 2-digit numbers, no regrouping.	A-50 Measure to the heatest commenter with the
A-26 Not tested in this level.	Total score (out of 44 possible)

Grade 1

Student Progress Report (List of Objectives)

This page is in the Teacher Manual and in the Test Assessment Pack. It lists each skill alongside an objective number. This page provides the foundation for tracking a student's achievement and may be sent home as a report card.

Tracking Achievement



Testing

The Test Assessment Pack contains 20 Pre-Test and 20 Post-Test booklets. Each test has 44 questions, one for each objective.

The number of each problem on the test matches the corresponding objective number of the opposite page.

Grade

Testing

Teachers see a snapshot of each student and the class at the beginning and end of the session.

s correct, leave the si on <u>missed</u>objec Teachers mark an X under the number of each problem the student misses. The total correct on the Pre- and Post-Test is recorded at the far right.

Grade

Teacher Guide

This lesson directs exploration with base ten blocks to discover a fundamental concept: ten of one place value equals one of the next higher place value.

Friendly Lesson Plans

Objective: To develop an understanding that 10 ones have the same value as 1 ten.

Materials: Base ten blocks (ones and tens), 6-sided dice, plastic bags, paper clips

Vocabulary: Ones, units, tens, long

Introductory Activities

Exploring and Discovering Patterns

Each pair should have 25 ones blocks and 10 tens blocks. Allow a short exploratory period. Children might make buildings, roads and parking ramps. Have students share their

Encourage children to look for patterns. These discoveries. blocks are important because of the pattern used to make them. We can find important patterns if we ask ourselves how these blocks are all the same and how they are different. Write 2 columns on the board: How are the

blocks the same? How are the blocks different?

Talk with your partner about ways the blocks are alike or the same. Think of a way to record what you find. You can draw a picture or write a word. What is a way the blocks are the same? (e.g. same material.) Write the answer under the word "same" on

the chalkboard. Now find other ways they are alike. (smooth, have 8 points, 6 sides, slide, stack, same color, solids, all made of little cubes)

Ask how the blocks are different. (different size, length, weight) How many different sizes do you have? (2) Can you put 1 of each size in front of you? We call the smallest block the "ones" or "units" block. What is the relationship or pattern between the ones block and the other block? (It takes 10 ones blocks to make the next block.) We will name the next size of block the "tens" or "long" block.

About This Page

Read the example together. Use base ten blocks to show that 10 ones are the same as 1 ten. Look at Problem 1. Match 1 block to each picture of a block. Do you have 10 or more blocks? (yes) Trade 10 ones for 1 ten. What blocks do you have now? (1 ten and 4 ones) Ring groups of 10 blocks. How many groups of 10? (1) Write a 1 in the blank above the

Students learn that each number from 11 to 20 can be shown as ones or a combination of 1 ten and additional ones.



word "tens." How many leftover ones blocks? (4) Write 4 in the blank above the "ones." What is another name for 1 ten 4 ones? (14)Have children complete the page on their own.

Follow Up Activities

SPIN TO 10

Each pair should have a die, 10 ones blocks and 1 tens block. Each pair puts a pile of ones blocks in the center of the play area. The tens block is put by itself and shared between players. Player 1 throws the die, removes the number of

ones from the pile, and places them by the tens block. Placing the ones blocks next to the tens block helps children see relationships, e.g. a 9 looks like 10 – 1 rather than 1, 2, 3, ... 9.

The winner is the first player who throws a number exactly to 10. (If a player has 9 ones and throws a 3, the player loses that turn. The player must spin "1" to get to 10 exactly.)

Journal Prompt List the numbers from 11 to 20. Draw a picture showing how many tens and ones are in each number.

1E Teacher Guide 29

Math games for partners and small groups reinforce the concept.

Test Preparation

Daily Review 15



Class starts with a five-question review from the back of the student book. Teachers review and discuss answers.



Grade

Test Preparation

Daily Reviews are the keys to long term retention.

Teachers report high satisfaction with use of Daily Reviews.

	Program	Ob	jectives
--	---------	----	----------

Grade



List of Objectives

k an X in the Pre- and/or Post-Test boxes to indicate missed objective	School
ident	
	à ch ^à
the rest of the second se	A ^{CC} Q ^{CE}
4° 4°	A-26 Subtract a 2-digit number from a 2-digit
Numeration	number, with regrouping.
A-1 Match objects \leq 9 with numerals.	A-27 Estimate and solve subtraction word
A-2 Order numerals 0-9.	problems.
$ \Box A-3 \qquad Use <, =, or > to compare out < 10 objects. $	A-29 Solve a subtraction word problem and of "How many more?"
A-4 Write the numeral from tens and ones blocks.	A-30 Skip count by 2's, 5's, 10's to 100.
A-5 Write the numeral from numerous, some	A-31 Divide a group of objects into equal groups,
Write five numbers before or after	none remaining.
any number < 100.	Fractions, Geometry, modern problem.
A-7 Write any humeral up to three of printed words.	A-32 Identify <i>top</i> and <i>bottom</i> and <i>bott</i>
A-8 Read and write words for any 3-digit numeral.	A-33 Identify <i>between</i> in a location problem.
A-9 Order and compare numbers to 999. Compare	A-35 Identify <i>next to</i> in a location problem.
number patients.	A-36 Identify above and below in a location
A-11 Compare objects as largest or smallest.	problem.
A-12 Order five different lengths from shortest	A-37 Identify a circle from a set of figures.
to longest.	A-39 Identify a triangle from a set of figures.
A-13 Identify ordinal poeters.	A-40 Identify a rectangle from a set of rightee.
	A-41 Identify portions of a region divided into
Operations	thirds or fourths.
\square \square $A-15$ Add sufficiences < 10 in horizontal or	A-43 Select two figures with the same shape.
vertical format.	A-44 Select two figures with the same shape
Add two or three numbers, sums a re-	A-45 Select two lights with the
Add sums < 10.	A-46 State the value of coins $< 9c$. Identity the
A-19 Submat a first and 1 digit,	penny and nickel.
no regrouping.	Identify the dime.
Add two numbers, both the sums < 90.	A-48 State value of coins and bills < 52.00 . Referring the guarter and half-dollar.
Add two numbers, 2 digits each,	A-49 Tell time in hours and half hours. Interpret a
no regrouping.	calendar.
no regrouping.	A-50 Measure to the nearest unit. Measure to the
Add two numbers, 2 digits each,	Total Score (out of 50 possible)
A-25 Subtract a 2-digit number from a 2-digit	
number, no regrouping.	50 50
	Assessment

Student Progress Report (List of Objectives)

This page is in the Teacher Manual and in the Test Assessment Pack. It lists each skill alongside an objective number. This page provides the foundation for tracking a student's achievement and may be sent home as a report card.

Tracking Achievement



Grade



Testing

Teachers see a snapshot of each student and the class at the beginning and end of the session.

ve the space empty.

Grade



Teacher Guide

As students discover different ways to solve a subtraction problem, they gain self confidence in their own ability to solve problems.

A major reason for errors in computation is a lack of understanding of multi-digit numeration. Students use base ten blocks to understand place value concepts.

Friendly Lesson Plans

Objective: To use base ten blocks to subtract 2digit numbers, no regrouping. To find a pattern for subtracting 2-digit numbers.

Materials: Place Value Mat (Master 10 and 11), base ten blocks (tens and ones), tape recorder (optional), 6-sided dice or playing cards.

Introductory Activities Each pair or group should have a Place Value Mat and base ten blocks. Today I will tell stories and record them on the tape recorder. Listen to the whole story the first time. Look for the question and needed facts. Discuss with your partner how to solve the problem. Next I will retell the story and pause after

each sentence for you to decide what to do. We will use the Place Value Mat and base ten blocks to solve the problem.

After you have found the answer with blocks, think of a way to record the story with paper and pencil.

Story 1: You buy a box of 78 peanuts at the circus. You eat 34 peanuts. How many peanuts do you have left?

Start by building Ones 7 tens and 8 ones. Tens 0 0 0 0 0 0 0 0 Then remove 3 tens Ones and 4 ones. Tens a a a a 0000 44 are left 4 ones 4 tens Students might record by drawing a picture

using sticks or dots for tens and ones, or they might record: 78 34

ΔΔ

pattern for subtracting two 2-

Possible explanations or patterns: 30 from 70 and 4 from 8 and 48 - 4 is 44 nd 8 - 4 is 4, so the answer is 44. umber in the ones place. Activity: Tell the students that tonight mbers in the tens place. Acuvuy: Let the students that tonight the old shepherd has 100 sheep to count. ve 79 hot dogs. You sell 28 y hot dogs do you have?

You can use base ten blocks on a Place Value Mat. 47 bears are under the Big Top. 23 bears leave How many bears are w many bears are der the Big Top? ove the sma read the number left ret build the large ONES ONES TENS 24 ล่อด - 23 vith pape Now work the problem u 7 Subtract 47 -23 the tens -23 the one 24 plocks to subtract. Cr X X X X X 3 000 2. 49 an**x**ano an**x**ano - 12 (1111111) 23 (111) -<u>35</u> 14 46 (()()()) - <u>20</u> 26 © 1998 Math Teachers Pr Page 49 Story 3: You have 75 peanuts. Your friend

Bill has fewer peanuts than you do. How many fewer peanuts does Bill have? (not enough information)

About This Page

Work the example at the top of the page together. Have students use base ten blocks. What is the pattern for subtracting 2-digit numbers? (Subtract the ones, then subtract the tens.) Have students complete the page.

Follow Up Activities

BINGO Skill Builders 25-3

Journal Prompt

Pat has 25 tickets. He uses 13 of them to go on a ride. How many tickets does he have left? Draw pictures of base ten blocks to solve and to explain your answer.

kill Builders 25-1, 25-2

2E Teacher Guide

49

Students find there are often many ways to solve the same problem. They naturally begin looking for the most efficient way—subtract the ones then subtract the tens.

Page 24

Summary: An old shepherd who counts

Summary: An Old Snepherd Who counts sheep to fall asleep has a troubled dream

Counting Sheep, Mendoza, George

about one to twenty sheep.

Test Preparation



Grade



Test Preparation

Daily Reviews are the keys to long term retention.

Teachers report high satisfaction with use of Daily Reviews.

Program Objectives

List of Objectives

Grade

dent Progress hopest to indicate missed objective	es. Teacher
n X in the Pre- and/or Post-rest bolies	School
ent	
	*
·	
\$ }	e e e e e e e e e e e e e e e e e e e
2°	B-28 Not tested in the set
Numeration	B-29 Donno and
B-1 Identify the plate B-2 Compare and order numbers up to 6 digits.	Rational Numbers
B-3 Complete patterns of multiples.	B-30 While the internet of a set, whole figure.
B-4 Write a numeral from printed words.	B-31 Write the fraction for the shaded part of a cost
B-5 Write the words for a number of a function of the place value in a 6-digit number.	B-32 Compare fractions less that 72 to w
B-b Identify the place	B-33 Not tested in this level.
B-8 Round to the nearest hundred.	B-34 Not tested in this level.
B-9 Find the missing number in an addition con-	Coometry
tence.	B-35 Not tested in this level.
Addition	B-36 Not tested in this level.
B-10 Add 3-digit numbers with 2 regress 5	B-37 Identify types of lines.
$\mathbf{B-11}$ Add there of roat 2 2 3	B-38 Identify a line of symmetry.
B-12 Not tested in this level.	B-39 Identify solid figures.
B-14 Define the word "sum" and the + sign.	B-40 (dentify
Subtraction	Measurement
B-15 Subtract 3-digit numbers with 2 regroupings.	B-41 Tell time to 5 minutes. B-42 Read a thermometer, scale and calendar.
B-16 Not tested in this level.	B-42 Reasure to the nearest $\frac{1}{2}$ inch or .5 cm.
B-17 Subtract 5-digit number across 0.	B-44 Recall equivalence of customary units of
B-18 Not tested in this level.	length, weight and capacity.
B-19 Define the word "difference" and the	weight and capacity.
Multiplication	B-46 Find the perimeter of a polygon. Find area.
B-20 Know multiplication facts up to 9 s.	B-47 Make change for \$10.00.
B-21 Multiply a 3-digit fullible by a + aligned across zero.	Problem Solving
B-22 Not tested in this level.	B-48 Solve a word problem with multiplication.
B-23 Not tested in this level.	B-49 Solve a word problem with division.
B-24 Define the word "product and the X sty	B-50 Read and interpret a graph.
Division	Total Scores (out of 38 possible)
B-25 Know division facts with divisors 0 to 9.	
B-26 Divide a 2-digit by a 1-digit fiduces in	38 38
B-27 NOT TESTED IN THIS IS AN	

Student Progress Report (List of Objectives)

This page is in the Teacher Manual and in the Test Assessment Pack. It lists each skill alongside an objective number. This page provides the foundation for tracking a student's achievement and may be sent home as a report card.

Tracking Achievement



Testing

The Test Assessment Pack contains 20 Pre-Test and 20 Post-Test booklets. Each test has 38 questions, one for each objective.

The number of each problem on the test matches the corresponding objective number of the opposite page.

Grade



Testing

Teachers see a snapshot of each student and the class at the beginning and end of the session.

Class Record Sheet

Results show improvement for each student and the class.

			neet	.cdoner.			· If answer is correct to-	
Student Name Numeratio	Addition	Subtraction	Multiplication	Grade:	School:		Put an X on missed obje	ectives.
1. Pre- 1 2 3 4 5 6	7 8 9 10 11 12 13 1	4 15 16 17 19 10	multiplication	Division	Rational Numbers	Geometry	Measurement	Problem Provide Must
2. Pre-			20 21 22 23 24 2	5 26 27 28 29	30 31 32 33 34 35	5 36 37 38 39 40	41 42 43 44 45 46 47	Solving Trect out of 50
3. Pre- Post-		티티티						/50 /50
4. Pre- Post-		EEE	# #	\Box				150
6. Pre-		日日日		\exists				/50
7. Pre-		884						/50
8. Pre-		5 5 F	Ξ Ξ					/50
9. Pre- Post-		리티브		3 #	++-			/50
10. Pre- Post- Z		- FI FF						/50 /50
11. Pre- 9 Post	No.	NOT NOT	- ğ	3	Z			/50
Pre- 07 Post- 10								/50
Post- 14. Pre-		- 8 - 8	8		TE			/50
Post-] [] []	- ++					/50
6. Pre- Post-				1 + +				/50
7. Pre- Post-								/50
8. Pre- Post-	Teache	ers mark	an X ur	nder th	ie numbe	er		/50
Pre- Post-	of eacl	of each problem the student misses. The					/50	
110-	total c	total correct on the Pre- and Post-Test is				/50		
	record	recorded at the far right.			/50			
	l							





Teacher Guide

"What you have been obliged to discover by yourself leaves a path in your mind which vou can use again when the need arises." —G.C. Lichtenberg

Friendly Lesson Plans

Objective: To round to the nearest ten, using a model.

Materials: Base ten blocks, interlocking cubes, real or play coins (Master 9)

Vocabulary: round

Introductory Activities

Rounding Pattern Write on the board: There are 28 students in Room 114, 21 students in Room 115 and 25 students in Room 116. About how many students are in each room?

Have students use base ten blocks to discover a pattern for rounding each number.

We round numbers to find out "about how much" a number is. Build the number 28. (2 tens blocks and 8 ones blocks) About how many tens would you say 28 is? Have students skip count by tens from 10 to 100. Place the number 28 between 20 and 30. Twenty-eight is between 2 tens and 3 tens. Build 2 tens and build 3 tens. Is 28 closer to 20 or 30? Work with your

partner to decide if 28 is closer to 20 or 30 and how you know. (It is closer to 30 because it would only take 2 more ones blocks to get to 30, but it would take 8 fewer blocks to get to 20. 28 is more than halfway between 20 and 30.)

Repeat with 21 and 25. Students should discover that numbers above the halfway number are "rounded up" and numbers below the halfway number are "rounded down."

Point out that the halfway number, 25, is

"rounded up" by agreement. This pattern also makes the rounding rule fair because five of the numbers in the twenties will round to 20 (20, 21, 22, 23, 24) and the other five numbers will round to 30 (25, 26, 27, 28, 29).

About This Page

Read the top of the page together. Look at the first example. What number are we going to round? (17) Build 17 with your base ten blocks. We will round to the nearest 10. What tens blocks would 17 be between? (1tens block and 2 tens blocks) Which is it closer

to? (2 tens, or twenty) How do you know? (It is more than the halfway number.) Go through the second example together,

explaining again that 15 is the halfway number, so

Rounding to the Nearest Ten with Base T Sounder an entry of not need an exact answer. Numbers can be conded of to find an exprovement Example: Round 17 to the nearest 10.	The Blocks by equal to the exact number. by answer:
Round 15 to the nearest ten.	Duild a Di train and a Di train Di la a la Strain Vio a la la Norman We could halfway multer ay:
Use base ten blocks to round each number 1. 10 3. 30 5. 61 60 6. 87 8. 25 30 9. 96 11. 40 12. 65 14. 80 80 15. 48	ar to the nearest ten. Look for a pattern. 2. 4. 100. 90. 7. 100. 100. 70. 13. 27. 30. 100. 100. 100. 100. 100. 100. 100. 100. 100. 100. 100. 100. 100. 100. 100. 100. 100.
0 Math Toschev ⁴ Paus Inc. Repr	dention by any materia defectly probability.

it is rounded up. Work through problems 1, 3 and 5 in the same way. Then have student pairs use base ten blocks to solve the remaining problems at the bottom of the page. Remind them that they are rounding to the nearest tens block.

Follow Up Activities

Rounding Money Write 43¢ on the chalkboard. Display 43¢ with dimes and pennies. If we round 43¢ to the nearest dime, how many dimes is it closer to? (4 dimes) Repeat with 41¢, 42¢, 44¢, 46¢...49¢. Write 45¢ on the chalkboard. What number of dimes is it closer to? (neither; halfway) We gree that the halfway number is to be rounded up. Point out that there are 5 amounts with a 4 in the tens place which round down (40¢ to 44¢) and 5 which round up (45¢ to 49¢).

Journal Prompt Round the number 76 to the nearest 10. Prove why it is nearest to that Use words, pictures and symbols to number. explain.

Skill Builders 7-1

3E Teacher Guide

Estimation is a difficult skill for many students. In this activity, students discover the pattern for rounding on their own.

Test Preparation



Easy Reteaching

Reteaching is a snap. Teachers can track each student's progress and pinpoint weak areas. Reproducible *Skill Builders* pages (shown here) for every objective are found in the Teacher Manual.

> This page reteaches objective 41 and is the first page for reteaching that objective.

Grade



Test Preparation

Daily Reviews are the keys to long term retention.

Teachers report high satisfaction with use of Daily Reviews.



Grade



List of Objectives

Program Objectives

lent	à vi ^à
in the	A ^{EC} A ^{CC}
40 ⁶	B-28 Divide a 4-digit by a 1-digit number, 0's in the
Numeration	quotient.
B-1 Identify the place value in a 3-digit numbers	Betional Numbers
B-2 Complete patterns of multiples.	B-30 Write the fraction for the shaded part of a
B-4 Write a numeral from printed words.	whole figure.
B-5 Write the words for a man B-6 Identify the place value in a 6-digit number.	B-31 While the modulo $1/2$ by fractions B-32 Compare fractions less than $\frac{1}{2}$ to fractions
B-7 Round to the nearest ten.	more than $\frac{1}{2}$.
B-8 Round to the means financial B-8 Find the missing number in an addition	denominators.
sentence.	B-34 Add or subtract 2 mixed functions and denominators.
Addition	Geometry
B-10 Add 3-digit numbers with 2 regroupings.	B-35 Identify plane figures.
B-11 Add times of four the unbers.	B-36 Identify and draw line position.
B-13 Add up to 5 numbers of differing lengths.	B-37 Identify a line of symmetry.
B-14 Define the word sum and	B-39 Identify congruent figures, name polygons.
Subtraction	B-40 Identify solid lightes.
B-16 Subtract 3-digit numbers with regroupings	Measurement
across 0.	B-41 Tell time to 5 minutes.
across 0.	B-43 Measure to the nearest ½ inch or .5 cm.
B-18 Subtract number of the year and the "–" sign	B-44 Recall equivalence of customary states length, weight and capacity.
Multiplication	B-45 Recall equivalence of metric units of length,
B-20 Know multiplication facts up to 9's.	weight and expansion of a polygon. Find area. $\mathbf{B-46}$ Find the perimeter of a polygon. Find area.
B-21 Multiply a 3-digit number by a + big across zero.	B-47 Make change for \$10.00.
B-22 Multiply a 2-digit number by a multiple of a multip	ber Problem Solving
B-23 Multiply a 2-digit futuriou by a with regrouping.	B-48 Solve a word problem with multiplication.
B-24 Define the word "product" and the X sign	B-49 Solve a word problem man
Division	
B-25 Know division facts with divisors o to or	Total Score (out of 50 possible)

Student Progress Report (List of Objectives)

This page is in the Teacher Manual and in the Test Assessment Pack. It lists each skill alongside an objective number. This page provides the foundation for tracking a student's achievement and may be sent home as a report card.

Tracking Achievement



Grade



Testing

Teachers see a snapshot of each student and the class at the beginning and end of the session.

Teachers mark an X under the number of each problem the student misses. The total correct on the Pre- and Post-Test is recorded at the far right.

Page 31

Grade

Teacher Guide

Students develop an understanding of the meaning of multiplication and division as opposite operations.

Friendly Lesson Plans

Objective: To use models to relate multiplication and division as opposites.

Materials: Base ten units blocks, interlocking plastic cubes, number line (Master 12), soft ball

Introductory Activities

Relating Multiplication and Division

Review the meaning of multiplication as putting together groups of equal size by acting out

Jane, Jack and Kim, would you each bring a problem.

4 books and place them on a pile on my desk? How many books are on my desk? (12) How did you get the answer? (skip counting by 4's or multiplying 3 x 4) The answer could be found by adding groups of equal size or

Write on the board: 4 + 4 + 4 = 12 or multiplying. $3 \ge 4 = 12.$

Show that division is the opposite of multiplication by putting the 12 books together in one pile. Then ask one student at a time to each remove 4 books from your desk. How many students removed groups of 4 books each? (3) How did you get your answer? (I watched the

problem being acted out and I saw that 4 could be subtracted three times.)

Write on the board: Multiplication and division are opposites. Multiplication puts together groups of equal size. Division takes apart groups of equal size.

About This Page

Use base ten blocks to demonstrate the relationship between multiplication and division

for several of the examples. Point out that students could write two different division facts for each given multiplication fact.

Follow Up Activities

Division on the Number Line

Mount a number line (made on page 25) on the wall. Pretend you have a board 12 feet long. You want to cut 4-foot shelves. How many shelves can you cut? Place 12 cubes above the number line. Remove 4 cubes at a time, showing 3 groups of 4.

Relating Multiplication and

Division Game Divide students into small groups of 4 to 6 students. A player in the middle throws a soft ball to a player in the outer circle saying a multiplication fact at the same time, "6 times 8..." The other player catches the ball and says the answer, "48," and throws the ball back to the center, saying a related division fact at the same time, "48 divided by 6...".

Journal Prompt

Skill Builders 25-2

4E Teacher Guide 38

> Student journal writing helps teachers understand students' thinking.

Test Preparation

Grade

Test Preparation

Daily Reviews are the keys to long term retention.

Teachers report high satisfaction with use of Daily Reviews. Grade

List of Objectives

Program Objectives

student Progress Report	Taocher
ark an X in the Pre- and/or Post-Test boxes to indicate <u>Inissed objectives</u>	
	School
itudent	x
	A COLOR
(e ² , 10 ² , 10 ²	o ^o
Pre \$ \$05 □	C-26 Add and subtract decimals of money
Numeration	C-27 Not tested in this level.
C-1 Identify the place value in a 7-digit number.	C-28 Not tested in this level.
C-2 Read, write and compare 9- digit humber	c-30 Not tested in this level.
C-3 Round to the nearest moustain.	a trace Measurement
C-4 Identify prime initiative, associative or the	Geometry & Weasurenter and
distributive property.	C-31 Identify a point, inter and angle
	C-32 Identify lines.
	C-33 Identify angles.
C-6 Add numbers up to 6-digits.	C-34 Identify basic shapes and solius.
L C-7 Subtract number by a 2-digit num-	C-35 Identify parts of a circle.
ber. Multiply by multiples of 10.	C-36 Measure to the heatest <i>y</i> and the second se
C-9 Divide a 6-digit by a 1-digit number.	angles.
C-10 Divide a 4-digit by a 2-digit number	C-38 Find the perimeter or area.
Fractions	C-39 Find the volume of a rectangular solid.
C-11 Write fractions from shaded regions, num-	C-40 Tell time to the nearest minute.
ber lines and printed words.	C-41 Use the appropriate unit for liquid capacity.
C-12 Find equivalent fractions	C-42 Use the appropriate and
and order 5 like or unlike proper fractions.	coins and bills; make change for a \$20 bill.
C-14 Interchange mixed numbers and improper	n them Solving
fractions.	Problem Solution
C-15 Add/subtract fractions with the denominators.	C-44 Gan filled the missing with
G-16 Add/subtract mixed numbers with common	whole numbers.
denominators.	C-46 Find the average of whole numbers of deci
C-17 Add/subtract unlike proper fractioner	mals.
C-18 Not tested in this level.	tables and charts.
C-19 Multiply 2 proper from rousening	C-48 Read and interpret line graphs and circle
C-20 Divide proper fractions by proper fractions	graphs.
or whole numbers.	Estimate sums and united at the state of the
Necimals	C-50 Estimate products of a 3-digit number.
c-21 Write decimals from a picture or from a	
number line.	Total Scores (out of 45 possible)
C-22 Read and write decimals up to thousandths.	
C-23 Identify place value up to the function of the second seco	45 45
C-24 Comparisonal Constant of the section of the	

Student Progress Report (List of Objectives)

This page is in the Teacher Manual and in the Test Assessment Pack. It lists each skill alongside an objective number. This page provides the foundation for tracking a student's achievement and may be sent home as a report card.

Tracking Achievement

Grade

Testing

Teachers see a snapshot of each student and the class at the beginning and end of the session.

Grade

Teacher Guide

Manipulatives increase visualization seeing math in the mind's eve. Retention increases 300% when students are able to visualize what they are learning.

Friendly Lesson Plans

Objective: To name fractions from fraction bars. To identify similarities and differences among fraction bars.

Materials: Fraction Bars[®], overhead Fraction Bars® (optional)

Vocabulary: fraction, similarities, differences, pattern

Introductory Activities

Discover the Concept of a Fraction Distribute a set of fraction bars to each group

of 2 to 5 students. Each fraction bar in this set represents one whole or one unit such as one whole cracker or one whole brownie. Look through your set of fraction bars with your group. Discuss in what ways your bars are all alike and in what ways they are different. Record your findings in a table with two columns headed "Similarities and Differences."

After 5-10 minutes, ask volunteers from each group to suggest the similarities and differences

colors

DIFFERENCES

different

color

divided into different

numbers of parts

number of shaded parts is

number of bars of any one

they have found. SIMILARITIES same shape same size congruent same width/length same area/perimeter same thickness same weight same material

*all divided into parts of equal size

*It is very important that the last similarity, i.e each bar is divided into parts of equal size, be verbalized. This is the essential concept of a fraction. To guide this discovery, ask What do the lines do to the fraction bar? (divide the bar into parts of equal size)

What's My Secret?

With a partner or small group, students take turns selecting a subset of fraction bars which are alike in one ans way. Others in the group try to guess the secret. Demonstrate an example by showing all the bars of one color and have students guess the secret of

28 5E Teacher Guide

Math games require students to apply their knowledge to "stump" their partner.

the sorting. Other ways the students will sort by: everything shaded, nothing shaded, one part shaded, equivalent parts (such as ¹/₂, ²/₄, ³/₆, ⁵/₁₀, ⁶/₁₂) shaded, more than $\frac{1}{2}$ shaded, and so on.

About This Page

This page provides examples of ways students may have sorted their fraction bars. Students generalize how three fractions are alike according to some attribute. Illustrate the first problem with overhead fraction bars or by drawing a picture.

Follow Up Activities

Journal Prompt

- Draw a picture and use symbols to
 - illustrate what Jon did each time.
 - 1. Jon cut his whole pizza into 4 slices of equal
- size. What fraction is one slice?
- 2. Jon cut 1 slice into 2 smaller parts of equal size.
- What fraction names the smaller part?

Skill Builders 11-1, 11-2

As students answer the question "How are these bars alike and how are they different?" they discover the essential concept of a fraction—a whole divided into parts of equal size.

Test Preparation

Grade

Test Preparation

Daily Reviews are the keys to long term retention.

Teachers report high satisfaction with use of Daily Reviews.

Grade
6

List of Objectives

Program Objectives

the contract of the pre- and/or Post-Test boxes to indicate missed objectives.	Teacher
	School
tudent	à
Perform	 C-26 Add and subtract decimals or money. C-27 Multiply money and 2-place decimals. C-28 Divide money and 2-place decimals. C-29 Identify the percent of shaded regions. C-30 Interchange 2-place decimals with fractions. Geometry & Measurement C-31 Identify a point, line, line segment, ray and angle.
Whole Number Operations	C-32 Identify lines.
C-6 Add numbers up to 6-digits. C-7 Subtract numbers up to 6-digits. C-8 Multiply a 3-digit number by a 2-digit number. D C-9 Divide a 6-digit by a 1-digit number. C-10 Divide a 4-digit by a 2-digit number. Fractions C-11 Write fractions from shaded regions, number lines and printed words. C-12 Find equivalent fractions. C-13 Compare 2 like or unlike proper fractions	 C-33 Identify angles. C-34 Identify basic shapes and solids. C-35 Identify parts of a circle. C-36 Measure to the nearest ⅓ unit. C-37 Use a protractor to measure and draw angles. C-38 Find the perimeter or area. C-39 Find the volume of a rectangular solid. C-40 Tell time to the nearest minute. C-41 Use the appropriate unit for weight. C-42 Use the appropriate unit for liquid capacity.
and order 5 like or unlike proper industrial	C-43 Give the total value of a container \$20 bill.
image: fractions. image: fractions. image: fractins. image: fractins. </td <td>Problem Solving □ C-44 Can find the missing number in patterns. □ C-45 Can solve a 1-step word problem with whole numbers. □ C-46 Find the average of whole numbers or decimals. □ C-47 Read and interpret pictographs, bar graphs, tables and charts. □ C-48 Read and interpret line graphs and circle graphs. □ C-49 Estimate sums and differences of numbers</td>	Problem Solving □ C-44 Can find the missing number in patterns. □ C-45 Can solve a 1-step word problem with whole numbers. □ C-46 Find the average of whole numbers or decimals. □ C-47 Read and interpret pictographs, bar graphs, tables and charts. □ C-48 Read and interpret line graphs and circle graphs. □ C-49 Estimate sums and differences of numbers
Decimals	C-50 Estimate products of a 3-digit number.
Image: C-21 Write decimals up to thousandths. Image: C-22 Read and write decimals up to thousandths. Image: C-23 Identify place value up to ten-thousandths. Image: C-24 Compare/order decimals up to hundredths. Image: C-25 Interchange fractions having denominators	Total Scores (out of 50 possible)

Grade 6

Student Progress Report (List of Objectives)

This page is in the Teacher Manual and in the Test Assessment Pack. It lists each skill alongside an objective number. This page provides the foundation for tracking a student's achievement and may be sent home as a report card.

Tracking Achievement

Testing

The Test Assessment Pack contains 20 Pre-Test and 20 Post-Test booklets. Each test has 50 questions, one for each objective.

The number of each problem on the test matches the corresponding objective number of the opposite page.

Grade

Testing

Teachers see a snapshot of each student and the class at the beginning and end of the session.

Class Record Sheet

Results show improvement for each student and the class.

Grade

Teacher Guide

Friendly Lesson Plans

Objective: To identify angles as right, acute, obtuse or straight.

Materials: Geoboards (or Master 12), masking tape, overhead geoboards (optional)

Vocabulary: right, obtuse, acute, straight, congruent

Geoboard Activities

Using a 25 peg geoboard, put a strip of masking tape below each row of pegs. Starting at the top left peg, write the letters A-E below each peg in the first row, F-J below each peg in the second row, K-O in the third row, P-T in the fourth row and U-Y in the bottom row. Use an overhead geoboard to demonstrate and to parallel the activities with the students.

-			•	•
•	B	С	D	Е
A			•	•
F	G	н	I	1
	•	•	•	•
ĸ	L	м	N	0
		•	•	•
P	0	R	S	Т
				•
L.	v	w	х	Y

Have students find and label a pair of line segments that are the same length. These line segments are congruent. Show an angle on a geoboard. Name another angle that is congruent. Prove they are congruent by using Master 12 and cutting out the first angle and placing the cutout on the other angle.

Geoboard Activities

Draw a right angle HRT on the chalkboard or overhead geoboard. Have students form the angle on their geoboards. Describe ∠HRT. (A right angle an angle with square corners, sides HR and RT are perpendicular.)

Draw an acute ∠JRT on the chalkboard. Have students form the same angle on their geoboards, using a contrasting color to ∠HRT.

How does ∠JRT compare to ∠HRT? (has a smaller measure) Is (JRT more than, less than or equal to 90°? (less than) Estimate the measure of $\angle JRT.$ (45°) Angles measuring less

than 90° are called acute angles. Draw ∠GRT on the chalkboard and repeat the

activity to identify obtuse angles as measuring more than 90°.

6E Teacher Manual 52

Draw ∠PRT on the chalkboard and repeat the activity to define a straight angle as two right

angles of 90°, each or 180°. Using the circular side of the geoboard, have students form $\angle BOD$ and describe the angle as

acute, right or obtuse. Repeat with $\angle BOH$ (straight) and $\angle BOF$ (obtuse).

Have students use toothpicks or straws to demonstrate angles equal to 90°, less than 90°, more than 90°, and equal to 180°.

About This Page

Ask students to study the two right angles drawn in the first illustration. How does the size of the second angle compare to the size of the first? (same) How do you know? (The small box always means 90°; the size of the angle does not change as the whole angle is rotated.)

Follow Up Activities

Journal Prompt

Think of the three types of angles: right, obtuse and acute. Explain how these angles are different.

<

Skill Builders 33-1

Students use geoboards to show models of geometric concepts.

Test Preparation

Grade

Test Preparation

Daily Reviews are the keys to long term retention.

Teachers report high satisfaction with use of Daily Reviews.

			Grade 7
Student P	rogress Report	objectives.	Teacher
Mark an X in the Pr	e- and/or Post-Test boxes to indicate <u>mees</u>		School
Student			•••••••••••••••••••••••••••••••••••••••
		2 48	2000
x (s ⁵		ore post	•
1851 AL	ation		Geometry
	nows the four basic operations.		D-29 Know geometric symbols and harrise
	Nake a true statement using number properties.		D-30 Identify types of angles.
	Vrite the prime factors for numbers ≤ 20 .		D-31 Name types of polygons.
D D-4	dentify the place value of, read, write, compare		D-32 Identity congruent region
	and order numbers ≤ 12 digits to any place value.		D-33 Filld the moust of the
D-5	Round numbers ≤ 7 units to any processing the second se		Measurement
D-6	Give the value of and white an over a supervision in factored form and vice versa.		D-34 Measure time measurements.
		ΗĻ	D-35 Add, subtract in the appropriate unit of measurement and
Who	Add numbers of the same or varying lengths.		can estimate length, weight and capacity.
	Subtract numbers of any length.		D-37 Use a table to convert measurements.
	Multiply a 4-digit number by powers of 10.	Hi	D-38 Find perimeter.
	Divide a 5-digit number by powers of 10.	H	D-39 Find the circumference of a circle.
	ution Concents and Computations	Ē	D-41 Find the volume of a rectangular solut.
	Change a fraction to higher or lower terms.		Problem Solving
	12 Add and subtract unlike proper fractions.		D-42 Fill in a missing number in patients.
	13 Add or subtract mixed numbers.	Π	D-43 Can solve a 1- or 2-step word problem are of 2-step word problem are
	14 Multiply proper fractions.		whole numbers, nuclear
	-15 Multiply mixed numbers.		D-44 Estimate the average of whole numbers, decimals,
	-16 Divide proper fractions.		fractions of percent.
	-17 Divide mixed numbers.		D-46 Solve a word problem using a proportion with a
	lecimal Concepts and Computations	nare	rate, scale drawing or similar shapes.
)-18 Identify the place value of, read, while, comp		D-47 Determine the probability of a simple event.
	and order decimals up to the nearest unit, tenth,	hun-	Algebra and Computer
	D-19 Round a decimal to the nearborn dradth or thousandth.		D-48 Identify, compare, order and solve word proble
	D 20 Interchange decimals and fractions.		with integers.
닐님	n_21 Add and subtract decimals and money.		D-49 Use the Galicsian system of P
	n-22 Multiply decimals or money.	_	D-50 Solve a 1- or 2-step linear equation with one
	D-23 Divide decimals or money.	L	variable and whole number coefficients.
	D-24 Multiply and divide whole numbers and o	Inci-	
	mals by powers of 10.		Total Correct (Out of 50)
	Percent Concepts and Computation	ents.	
	D-25 Interchange fractions, decimals and percention	a. 5	50 50
	D-26 Find the missing number in a proportion	ole	
	D-27 Find the whole number percent of a with		
	number, decinar of filosount, sales tax	or inter-	
	D-28 Fille the amount of distance		

Student Progress Report (List of Objectives)

This page is in the Teacher Manual and in the Test Assessment Pack. It lists each skill alongside an objective number. This page provides the foundation for tracking a student's achievement and may be sent home as a report card.

Grade

List of Objectives

Tracking Achievement

Teachers mark an X under the number

recorded at the far right.

of each problem the student misses. The total correct on the Pre- and Post-Test is

each student and

Post

Pre-

TOTAL

the class.

Testing

Grade

Testing

Teachers see a snapshot of each student and the class at the beginning and end of the session.

Page 43

Record Nu

rrect out of 50

Teacher Guide

Students develop an understanding of volume by building a box from centimeter graph paper and filling the box with 1 centimeter cubes.

Friendly Lesson Plans

Objective: To find the volume of a rectangular solid.

Materials: Centimeter graph paper, centimeter cubes, scissors, tape, base ten blocks, one inch graph paper (Master 1)

Introductory Activities

A Cubic Centimeter

Each small group should have graph paper,

scissors and tape. Use your centimeter graph paper, scissors and tape to build a model of a cube measuring 1 cm on each edge. The space inside your cube is called its capacity or volume. The 1 cm cube has a volume of 1 cubic cen-

Write on the board: The volume of a 1 cm timeter. cube = 1 cubic centimeter (or 1 cu cm or 1 cm³)

Display 1 unit block from a set of base ten blocks. This block or cube is 1 centimeter on each edge. It is a 1 centimeter cube and has a volume of 1 cubic centimeter. Show a solid with a volume of 2 cubic centimeters. (2

cubes placed together) Have students build different models of solids having a capacity or volume of 4 cubic inches. Discuss how the models are alike and different. (They all have the same volume but have different shapes.)

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Next build a box that is 6 centimeters by 4 centimeters wide and 2 centimeters high. Find the number of cubic centimeters inside the box. Students should build the model with their graph paper to find the answer.

About This Page

Read the illustration together. Give each student a sheet of centimeter graph paper to build the box described. Fill the box with 1 cm cubes to find its volume.

Have students work with a partner to complete problems 1-8. Have one person build a model to match each picture and the other partner count the number of cubes needed to fill the model.

A Cubic Inch Use your one-inch graph paper, scissors and tape to build a model of a cube measuring 1 inch on each side. The space inside your cube is called its capacity or volume. A one-inch cube has a capacity or volume of 1 cubic inch.

Journal Prompt

Would you use perimeter, area or

- 1. the length of wood needed to frame a picture volume to measure: 2. the water needed to fill a bathtub
 - 3. carpet needed to cover the living room floor 4. fencing to enclose a small garden
 - Explain each of your answers by drawing and
- labeling diagrams.

Test Preparation

Grade

Test Preparation

Daily Reviews are the keys to long term retention.

Teachers report high satisfaction with use of Daily Reviews.

Program Ob	jectives Grade 8
Student Progress Report	tives. Teacher
Mark an X in the Pre- and/or Post loss and	School
Student	•••••
	a oo
	Geometry
Numeration	D-29 Know geometric symbols and names.
D-1 Know and dee and D-1 C D-2 . Make a true statement using number properties.	D-30 Identify types of angles.
D -2 Write the prime factors for numbers ≤ 20 .	D-31 Name types of polygons.
D-4 Identify the place value of, read, write, compare	D-32 Identify congruent rightes.
and order numbers ≤ 12 digits.	D-33 Find the fileasure of a miles in triangles.
D-5 Round numbers \leq 7 uights to any p	D-52 Knows the sum of angles
D-6 Give the value of and when and vice versa.	D-53 Identify corresponding
D-57 Use scientific notation.	U-54 Kilows the Fyrings
	Measurement
D-7 Add numbers of the same or varying lengths.	D-34 Weasure time we ultiply and divide measurements.
D-8 Subtract numbers of any length.	D-36 Estimate length, weight and capacity.
D-9 Multiply a 4-digit number by powers of 10.	D-37 Use a table to convert measurements.
D-10 Divide a 5-digit number by powers of res	D-38 Find perimeter.
Fraction Concepts and Computations	D-39 Find the circumterence of a circuit.
D-11 Change a fraction to higher or re-	D-41 Find the volume of a triangle or parallelogram.
D-12 Add an subtract mixed numbers.	D-55 Find the area of a circle.
D-13 Add of subsections.	D-bb Find the area of a size
D-15 Multiply mixed numbers.	Problem Solving
D-16 Divide proper fractions.	D-42 Fin in a moons of D-42 Fin in a moons of D-42 Fin in a moons of D-43 Cap solve a 1- or 2-step word problem using
D-17 Divide mixed numbers.	whole numbers, fractions or decimals.
Decimal Concepts and Computations	D-44 Estimate the answer by rounding.
D-18 Identify the place value of, reau, while, compare	D-45 Find the average of whole numbers, decimals,
and order decimals of to the nearest unit, tenth,	fractions or percent.
bundredth or thousandth.	D-46 Solve a word proton at a line shapes.

D-27 Find the whole number percent of a whole number, decimal or money amount. **D-28** Find the amount of discount, sales tax or Total Correct (Out of 60) interest in a percent problem. 60 60 **D-51** Find what percent one number is of another. Student Progress Report (List of Objectives)

hundredth or thousandth.

D-22 Multiply decimals or money. **D-23** Divide decimals or money. **D-24** Multiply/divide whole numbers and decimals

by powers of 10.

Percent Concepts and Computations

D-25 Interchange fractions, decimals and percents.

D-26 Find the missing number in a proportion.

D-20 Interchange decimals and fractions. **D-21** Add and subtract decimals and money.

This page is in the Teacher Manual and in the Test Assessment Pack. It lists each skill alongside an objective number. This page provides the foundation for tracking a student's achievement and may be sent home as a report card.

 \square

rate, scale drawing or similar shapes.

D-48 Identify, compare, order and solve word problems

D-58 Solve operations with rational numbers.

D-60 Identify output of a BASIC program.

D-59 Graph a linear equation. Use order of operations.

D-47 Determine the probability of a simple event.

Algebra and Computer

with integers. **D-49** Use the Cartesian coordinate system. D-50 Solve a 1- or 2-step linear equation.

Grade

List of **Objectives**

Tracking Achievement

Grade

Grade

Teacher Guide

"What you have been obliged to discover by yourself leaves a path in your mind which you can use again when the need arises." —G.C. Lichtenberg

Friendly Lesson Plans

Objectives: To square a number. To find the square root of a number. To find the Pythagorean relationship in right triangles.

Materials: Centimeter Graph Paper (Master 5), crayons, scissors, glue

Vocabulary: Square, squared, exponent, factor, square root, Pythagorean theorem, legs, hypotenuse, radical sign

Introductory Activities

Squaring a Number

Display a 1 centimeter square and describe the number of units on each side. This is the smallest square shape we can make with these squares. Each side of the square has a unit of 1. How many units on the horizontal side? (1) on the vertical side? (1) How many small squares in the whole figure? (1) Write on the board: The square of $1 = 1 \times 1 = 1$

Build the next smallest square shape. How many units on the vertical side? (2) How many units on the horizontal side? (2) How many small squares in the whole figure? $\left(4\right)$ Write on the board: The square of $2=2 \times 2=4$

Introduce the exponent as a shortcut way of expressing each relationship, e.g. $2^2 = 2 \times 2$ or 4. Have students continue the following table:

	Vertical by	Squares	<u>Relationship</u>
Units	<u>F10112011tai</u>	1	$1^2 = 1 \times 1 = 1$
1	1 by 1	1	1 - 1
1	0 100 9	4	$2^2 = 2 \times 2 = 4$
2	2 by 2	÷	
:	:		10 - 10 = 100
•	10 hr 10	100	$10^2 = 10 \times 10 = 100$
10	10 Dy 10		

Square Roots

54

Now we will undo squaring a number. We will build the squared number with small squares and then find how many units on each side to find the original number.

Build a square using exactly 9 of your small squares. How many small squares in the large square? (9) How many units on each side of the large square? (3) The number of units on each side is called

the square root. We say the square root of 9 is 3 and we write this relationship with a special symbol called the radical sign.

Write on the board: $\sqrt{9} = 3$

8E Teacher Manual

Discovering the Right Triangle Pattern

Each student will need a sheet of centimeter graph paper and base ten blocks. Have students outline and cut a square with 1 cm on each side, 2 cm ... 10 cm on each side.

Write on the board: How many right triangles can be formed by joining 3 different sides of your

Ask students to describe each right triangle 10 squares?

they find. (Students will find the 3-4-5 right triangles and the 6-8-10.) There is a pattern for the sides of every right triangle. The sum of the squares on the 2 small ends of a right triangle equals the square on the large side.

About This Page

Work the top of the page together, then have students complete the page on their own.

Follow Up Activities

Journal Prompt Evon said a triangle with units of 6 cm, 3 cm and 12 cm is a right triangle. Draw a picture of the trangle. Explain why you agree or lisagree with Evon.

In this lesson, students use squares of different sizes to discover the Pythagorean Theorem.

Test Preparation

Grade

8

Test Preparation

Daily Reviews are the keys to long term retention.

Teachers report high satisfaction with use of Daily Reviews. Spanish

Teacher Guide and Spanish Resource Pack

Teachers use both the English Teacher Guide and the Spanish Resource Pack.

The English Teacher Guide provides step-by-step directions for each student book page. The Spanish Resource Pack includes matching tests and Skill Builder pages in Spanish.

Student Books

Both English and Spanish speakers can work together in the same classroom. *Moviéndose con Matemáticas*[®] is an exact match to the English student book.

Boxed Class Kits in Spanish

A boxed class kit in Spanish includes:

1 English Teacher Manual

1 Spanish Resource Pack 20 Spanish student workbooks

20 Spanish Parent Handbooks

Getting Started in Spanish...

The Extensions series is made to fit seamlessly into any classroom, whether it's taught in English, part English and part Spanish, or entirely in Spanish. This program is ideal for second language and ELL students because

manipulatives convey the abstract concept even when students have difficulty understanding the spoken language.

Content-based instruction is combined with language development activities to increase ELL students' understanding of math concepts and skills.

The Grade 4 Pre-Test in Spanish tests the same objectives as the English Pre-Test shown on page 8.

The Spanish Resource Pack contains matching Pre- and Post-Tests plus Skill Builders reteaching pages and vocabulary words in Spanish. All are reproducible.

Matching Books

English and Spanish pages match exactly!

Easy Review and Reteaching in Spanish

Call 1-800-852-2435 to receive a copy of results achieved with second language students.

Spanish

Manipulatives Benefit ELL Students

Manipulatives are especially beneficial to second language learners. Manipulatives convey the concept even when language is not developed.

Illustrations connect the hands-on activities to practice pages.

Students work in small groups in an active language learning environment.

Response to Intervention

Moving with Math[®] materials integrate all eight of the Best Practices published by What Works Clearinghouse.

Moving with Math[®] **Extensions** addresses all the essential math content standards for grades K through 8. *Moving with Math*[®] **Extensions** is **RTI Ready**[™] and includes all of the recommendations listed below.

"RTI intentionally cuts across the borders of special education and general education and involves school-wide collaboration."

Assisting Students Struggling with Mathematics: Response to Intervention (RTI) for Elementary and Middle Schools, National Center for Education Evaluation and Regional Assistance, 2009

Moving with Math® Extensions RTI Check List ✓

Predictive Screening:

▶ Pre-Tests, Post-Tests, Daily Reviews, and weekly Check Points identify at-risk students and monitor progress

In-Depth Instruction:

- ▶ Focus on whole numbers in grades 1 through 4
- ▶ Focus on rational numbers in grades 4 through 8 (decimals and fractions)

Systematic and Explicit Instruction:

- Lightly-scripted lesson plans guide instruction
- Classroom activities use explicit models and strategies
- Students given opportunities to verbalize, write, discuss, and practice skills learned

Solving Word Problems:

- Explicit steps and strategies for solving word problems
- Practice solving word problems using alternative strategies
- ▶ Use of word frames [underlying structures] in solving word problems

✓ Visual Representations of Math Concepts:

- Manipulative-based activities introduce each math concept
- ▶ Pictorial representations on every student page

✓ Fluency-Building Activities:

- **Skill Builder** worksheets include flash cards, timed exercises, speed games
- Include research-based strategies such as fact families

Monitoring:

Pre-Tests, Post-Tests, Daily Reviews, weekly Check Points, and embedded assessments monitor the progress of at-risk students

Motivation:

 Activity-based instruction offers rich opportunities for student success and natural occasions for praise and encouragement

Moving with Math[®] Foundations and Math by Topic (IM/MH) are also RTI Ready[™]. Visit our website to learn more.

www.movingwithmath.com